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2024-DSE MATH EP M1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY

HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2024

Please stick the barcode label here. Candidate Number

MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8:30 am – 11:00 am (2½ hours) This paper must be answered in English

INSTRUCTIONS

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of TWO sections, A and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown.
- (6) Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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SECTION A (50 marks)

1. The table below shows the probability distribution of a discrete random variable X, where a and b are constants such that 6 < b < 15.

x	0	3	6	<i>b</i> 8	15
P(X=x)	0.3	a _{0.2}	0.1	0.2	0.2

It is given that Var(5X) = 739. C

- (a) Find a and b.
- (b) Let C be the event that $0 < X \le 7$.
 - (i) Let D be the event that $4 < X \le 15$. Are C and D independent? Explain your answer.
 - (ii) Let E be an event such that $P(E) \neq 0$. If C and E are mutually exclusive, write down the greatest possible value of P(E).

(7 marks)

Answers written in the margins will not be marked.

$$\alpha = 0.2$$

$$E(x) = 0 + 3(0.2) + 6(0.1) + b(0.2) + 15(0.2)$$

$$= 0.26 + 4.2$$

$$Var(x) = 9(0.2) + 36(0.1) + b^{2}(0.2) + 225(0.2) - (0.2b + 4.2)^{2}$$

$$= 0.26^{2} + 50.4 - (0.046^{2} + 1.686 + 17.64)$$

$$0.16b^{2}-1.68b+3.2=0$$

ci)
$$P(C) = 0.2 + 0.1 = 0.3$$

$$P(D) = 0.1 + 0.2 + 0.2 = 0.5$$

$$P(C) \times P(D) = 0.3 \times 0.5 = 0.15$$

.. No. They are not.

The greatest possible value of P(E) = 0.3	ii) : P(CNE) = (_ 7
	The grea	test possible value of P(t)=	0. 3
			and an analysis of the state of
		\	

- 2. In an orchestra, $\frac{3}{5}$ of the members wear glasses. Among the male members, $\frac{4}{9}$ of them wear glasses. The probability that a randomly selected member is a female not wearing glasses is $\frac{3}{20}$.
 - (a) Given that a randomly selected member does not wear glasses, find the probability that the member is a female.
 - (b) Find the probability that a randomly selected member is a female wearing glasses.

a) Req. prob. = $\frac{\frac{3}{20}}{\frac{3}{1}}$ = 0.25

b) let \times be the prob. of female. $(\times)(\frac{3}{20}) = \frac{2}{5}(0.25)$ $x = \frac{2}{3}$

Answers written in the margins will not be marked.

The prob. of female = $\frac{2}{3}$ $\therefore \text{Req. prob.} = \frac{2}{3} \times (1 - \frac{3}{20})$ $= \frac{17}{30}$

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- 3. When a coin is tossed, the probability of getting a tail is p, where 0 . When the coin is tossed 20 times, the ratio of the probability of getting 1 tail to the probability of getting 3 tails is 49:57.
 - (a) Find p.
 - (b) The coin is tossed k times. Find the least value of k so that the probability of getting at least 1 tail is greater than 0.85.

(6 marks)

a)
$$\frac{C_{1}^{20}(p)(1-p)^{19}}{C_{3}^{20}(p)^{3}(1-p)^{17}} = \frac{49}{57}$$

$$\frac{20(p)(1-p)^{19}}{1140p^{3}(1-p)^{17}} = \frac{49}{57}$$

$$48p^2 + 2p - 1 = 0$$

$$P = \frac{1}{8}$$
 or $-\frac{1}{6}$ (rej.

b)
$$1 - C_0^k (\frac{1}{8})^0 (\frac{7}{8})^k > 0.85$$

 $(\frac{7}{8})^k < 0.15$

- 4. The weekly revision time of each student in a school follows a normal distribution with a mean of μ hours. A random sample of 81 students is drawn from the school. The mean and the standard deviation of the weekly revision time of these students are 13 hours and 1.75 hours respectively.
 - (a) The width of a β % confidence interval for μ is 0.7. Find β .
 - (b) It is given that there are 36 boys in the sample, and the mean and the standard deviation of the weekly revision time of these boys are 12.5 hours and 2 hours respectively. Find the standard deviation of the weekly revision time of the girls in the sample.

[Hint: The sample standard deviation is $\sqrt{\frac{1}{n-1} \left(\sum_{i=1}^{n} x_i^2 - n\overline{x}^2 \right)}$.]

(6 marks)

Answers written in the margins will not be marked.

a)
$$2 \cdot z \cdot \frac{1.75}{81} = 0.$$

b) let x be the mean of girls.

$$36(12.5) + (81-36)(x) = 81(13)$$

 $45x = 603$

- 5. Let n be a positive number.
 - (a) Expand $\frac{2}{e^{nx}}$ in ascending powers of x as far as the term in x^3 .
 - (b) Consider the expansion of $(1+4x)^m + \frac{2}{e^{nx}}$, where m is a positive integer. The coefficients of x and x^2 in the expansion are 24 and 980 respectively. Find the coefficient of x^3 in the expansion. (7 marks)

a)
$$\frac{2}{e^{hx}}$$

= $2e^{-hx}$
= $2(1-hx+\frac{n^2x^2}{2}-\frac{n^3x^3}{6}+...)$
= $2-2hx+h^2x^2-\frac{n^3x^3}{3}+...$
b) $(1+4x)^m+\frac{2}{e^{hx}}$

b)
$$(1+4x)^{m} + \frac{2}{e^{nx}}$$

 $= [1+4xm + \frac{m(m-1)}{2}(16x^{2}) + \frac{m(m-1)(m-2)}{6}(64x^{3}) + ...] + \frac{2}{e^{nx}}$
 $= 1+4xm + 8x^{2}m(m-1) + \frac{3^{2}}{3}x^{3}m(m-1)(m-2) + 2 - 2nx + n^{2}x^{2} - \frac{n^{3}x^{3}}{3} + ...$
 $= 3 + (4m-2n)x + (8m(m-1)+n^{2})x^{2} + (\frac{3^{2}}{2}m(m-1)(m-2) - \frac{n^{3}}{2})x^{3}$

$$= 3 + (4m-2n)x + (8m(m-1)+n^{2})x^{2} + (\frac{32}{3}m(m-1)(m-2) - \frac{n^{3}}{3})x^{3} + \cdots$$

$$\begin{cases}
4m-2n=24 - (1) \\
8m(m-1)+n^2=980 - (2)
\end{cases}$$

(1):
$$h = 2m - 12 - (3)$$

$$m = 11$$
 or $-\frac{19}{3}$ (rej.)

$$n = 2(11) - 12 = 10$$

-: coefficient of
$$x^3 = \frac{32}{3}(11)(11-1)(11-2) - \frac{10^3}{3}$$

= $\frac{30680}{3}$

6. (a) Let $e^u = (x^2 + x + e)^{2x}$	+1
---------------------------------------	----

- Express u in the form of $p(x)\ln(q(x))$, where p(x) and q(x) are polynomials. (i)
- Express $\frac{d}{dx}e^{u}$ in terms of x. (ii)
- The equation of the curve Γ is $y = (x^2 + x + e)^{2x+1}$. Denote the point of intersection of Γ and (b) the y-axis by H. Find the equation of the tangent to Γ at H.

(7 marks)

Answers written in the margins will not be marked

Inu = (2×+1)|n(x2+x+e)

$$\frac{d}{dx}e^{x} = \frac{d}{dx}(x^{2}+x+e)^{2x+1}$$

$$= (x^{2}+x+e)^{2x+1} \left[2\ln(x^{2}+x+e) + \frac{(2x+1)^{2}}{(x^{2}+x+e)} \right]$$

Slope of tangent =
$$(0+0+e)^{1} \left[2\ln(e) + \frac{(0+1)^{2}}{(0+0+e)} \right]$$

= $e\left(2 + \frac{1}{e}\right)$

$$= 2e + 1$$

Equation of tangent:

$$y-e = (2e+1)x$$

$$y = (2x+1)x + e$$

7.	A computer programme adjusts the length and the breadth of a rectangular digital picture, such that the length
	of its diagonal remains constant while its breadth decreases at the constant rate of 0.5 cm s ⁻¹ . Initially, t
	length and the breadth of the picture are 20 cm and 15 cm respectively. Denote the breadth of the picture
İ	by x cm. Find the rate of change of the area of the picture when $x = 7$. (4 mark

$$A = (x)(x+5) = 2x^{2} + 5x$$

$$\frac{dx}{dy} = -0.5 \text{ cm s}^{-1}$$

$$\frac{dh}{dx} = 4x + 5$$

$$\frac{dR}{dY} = \frac{dR}{dx} \cdot \frac{dx}{dy}$$
$$= (4x+5)(-\frac{1}{2})$$
$$= -2x-5$$

$$\frac{dH}{dV} |_{x=7} = -2(7) - \frac{5}{2}$$

$$= -\frac{33}{2} \text{ cms}^{-1}$$

	8.	(a)	Using the Standard Normal Distribution Table on page 24, evaluate	\int_0^0	$e^{\frac{-x^2}{2}}$	dx	•
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Consider the curve $C: y = (2x-1)e^{\frac{-x^2}{2}}$, where $x \ge 0$. Using the result of (a), find the area of the (b) region bounded by C, the x-axis and the y-axis.

(7 marks)

Answers written in the margins will not be marked.

a)
$$\int_{0}^{0.5} e^{-\frac{x^{2}}{2}} dx = 0.1915$$

b)
$$(2 \times -1) \cdot e^{-\frac{x^{*}}{2}} = 0$$

$$x = 0.5$$

$$\cdot \cdot \times - intercept = 0.5$$

$$= \int_{0.5}^{0.5} (2 \times -1) e^{-\frac{x^{2}}{2}} dx \qquad let u = -\frac{x^{2}}{2}$$

$$= \int_{0.5}^{0.5} 2 \times e^{-\frac{x^{2}}{2}} - \int_{0.5}^{0.5} e^{-\frac{x^{2}}{2}} dx \qquad \frac{du}{dx} = -x$$

$$dx = -\frac{1}{2} \cdot du$$

$$=-2\left[l^{4}\right]_{0}^{-0.125}-0.1915$$

$$= -2(e^{-0.125}-1) - 0.1915$$
$$= 1.8085 - 2e^{-0.125}$$

$$= 1.8085 - 2e^{-0.125}$$

Answers written in the margins will not be marked.

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SECTION B (50 marks)

- 9. The weight of each pumpkin in a large market follows a normal distribution with a mean of μ /kg and a standard deviation of σ (kg.) It is given that 30.85% of the pumpkins in the market each weighs more than 5.7 kg while 78.88% of the pumpkins each weighs between $(\mu - 1.5)$ kg and $(\mu + 1.5)$ kg.
 - Find μ and σ . (a)

(3 marks)

Answers written in the margins will not be marked

- Suppose that 16 pumpkins are randomly chosen in the market. Find the probability that the (b) mean weight of these pumpkins does not exceed 5.4 kg. (2 marks)
- (c) The following table shows the grades and the prices of the pumpkins in the market.

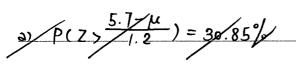
Weight of a pumpkin (Wkg)	<i>W</i> ≤ 3.6	$3.6 < W \le 5.7$	W > 5.7
Grade,	С	В	Α .
Price (\$)	50	80	100

011056

0,3085

Suppose that 8 pumpkins are randomly chosen in the market and these pumpkins are put into a trolley.

- Find the expected price of the pumpkins in the trolley. (i)
- Find the probability that there are at least 5 grade B pumpkins and at least 1 grade A pumpkin in the trolley.



(6 marks)

12

b) P(Z <	$\frac{5.4-5.1}{1.2}$) = P($z \le \frac{0.3}{0.3}$)
***************************************	$= P(Z \le I)$
	3.6-5.1
ci) P(Z<	$\frac{3.6 \text{ sy}}{1.2}$) = $P(Z \le -1.25)$ = $0.5 - 0.3944$
	= 0.1056
Expect	ed price = (8 × 0.1056 × 50)+ (8 × (1-0.1056-0.3085) × 8
	+ (8×0.3085×100)
	= \$664.016
ii) Req. p	rob. = $C_5^8 (0.5859)^5 C_2^3 (0.1056)^2 (0.3085) +$
***************************************	$C_6^8 (0.5859)^6 C_1^7 (0.1056)(0.3085) +$
	C7 (0.5859)'·C; (0.3085) +
	$C_{5}^{8}(0.5859)^{5} \cdot C_{2}^{3}(0.3085)^{2}(0.1056) +$
	$C_{5}^{8}(0.5859)^{5} \cdot C_{3}^{3}(0.3085)^{3}$
	= 0.4023
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Find the probability that a certain day is <i>smooth</i> . Find the probability that all the 7 days in a certain we	0 1 2	ay.
Find the probability that all the 7 days in a certain we		(2 marks
	eek are smooth.	(2 marks
Given that all the 7 days in a certain week ar exactly 10 delays in that week	re smooth, find the probabilit	y that there ar (4 marks
Given that there are no delays in at least 2 day all the 7 days in that week are smooth. Req. prob. = $e^{-1.6} \left(\frac{1.6^{\circ}}{0!} + \frac{1.6!}{1!} + \frac{1.6!}{2!} \right)$	ys in a certain week, find the $\left(\frac{6^2}{2!}\right)$	probability that (4 marks
= 0.7834 p		
Req. prob. = (0.7834)7		
= 0.1810 B		
1-e-11.210 \ 1 = 10	10 5.	
Reg. prob. = (-10!) - 8.18	70	
= 0.6465 c	,	
2-16162		
Prob. of no delay = 01		no delay
= 2-1.6		. 0
Dut of my later to the locate ?	1	
Prob. of no delays in at least $2 = 1 - C_0^7 (e^{-1.6})^{\circ} (1 - e^{-1.6})^7 - C_1^7$	1.6) (1 - 0 -1.6) 6	
= 0.4285	(e · ·)(1-e ·)	
	31 O	
Reg. prob. =		
	\	

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11.

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where a and b are constants, and t ($0 \le t \le 4$) is the number of hours elapsed since 7 am on that day. It is found that $\ln\left(\frac{P}{-t^2+10t+8}\right)$ is a linear function of t, and the graph of this linear function passes through the point (3, -0.1) and the intercept on the horizontal axis is 2.5.

- Express $\ln\left(\frac{P}{t^2+10t+8}\right)$ as a linear function of t. (1 mark)
- (b) Find the exact values of a and b. (3 marks)
- Using the trapezoidal rule with 4 sub-intervals, estimate the accumulative rainfall of city M (c) from 7 am to 11 am on that day. (2 marks)
- The accumulative rainfall of city N on the same day increases at a rate of Q mm per hour. It is given (d)

$$Q = \frac{16(2t+5)e^{0.4t}}{4te^{0.4t}+3} ,$$

where t ($0 \le t \le 4$) is the number of hours elapsed since 7 am on that day.

- Find Q dt. (i)
- Someone claims that the sum of the accumulative rainfalls of city M and city N from 7 am (ii) to 11 am on that day is greater than 160 mm. Do you agree? Explain your answer.

(8 marks)

a)
$$P = a(-t^2 + 10t + 8) e^{bt}$$

$$\frac{P}{-t^2 + 10t + 8} = a e^{bt}$$

$$\ln(\frac{P}{-t^2 + 10t + 8}) = bt + 1na$$
b) $b = \frac{o + o.1}{2.5 - 3}$

$$-o.1 = \frac{o + o.1}{2.5 - 3}$$

$$\ln\left(\frac{P}{-t^2+10t+8}\right) = bt + \ln a$$

b)
$$b = \frac{0+0.1}{2.5-3}$$
 $-0.1 = -0.2(3) + \ln a$

Let
$$f(t) = e^{0.6}(-t^2+10t+8)e^{-0.2t} = e^{0.2t}$$

c) $\Delta t = \frac{4-0}{4} = 1$ The end-points = 0 > 1 > 2 > 3 > 4

The accumulative rainfall =
$$\int_0^4 f(+) dt$$

= $\frac{1}{2} [f(0) + 2f(1) + 2f(2) + 2f(3) + f(4)]$

Answers written in the margins will not be marked

$\frac{16(2t+5)e^{0.4t}}{4te^{0.4t}+3}dt$	let u = 4te ^{0.4t} +3
311) 4te 33 + 3	$\frac{du}{dt} = 4e^{0.4t} + 1.6te^{0.4t}$
$= \int \frac{16}{0.8} \cdot u \cdot du$	$\frac{du}{dt} = 0.8e^{0.4t}(5+2t)$
= 20/n/4te°.4t + 3/ + C	
when $t=0$, $\int Q=0$	
20 n3 + C = 0	
C = -201	n3
$\int Q dt = 20 \ln 4te^{0.4t} $	+31-20In3
= 20/n(4te°.	$\left(\frac{a_t}{a_t} + \frac{3}{3}\right)$
(4 Q dt = [20 n/4te00	*t+3)
$= 20 \ln \left(\frac{16e^{1.6}}{2} \right)$	-3-)-20/n(1)
ii) $\int_{0}^{4} Q dt = \left[\frac{20 \ln \left(\frac{4t e^{0.6} + 1}{3} \right)}{20 \ln \left(\frac{16 e^{1.6} + 1}{3} \right)} \right]$ $= 20 \ln \left(\frac{16 e^{1.6} + 1}{3} \right)$	(+3)
≈ 66.2227 mm	3
Sum of accumulative rain	ifall of two city
= 66 . 2227 + 94, 1600	
= 160.3826 mm	
>160 mm	
-: Tes. I agree.	
	. •

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- Does the greatest rate of change of the total revenue of the shop exceed 4 thousand dollars per month? (a) Explain your answer. (4 marks)
- Let P be the total profit (in thousand dollars) of the shop. It is given that (b)

$$\frac{dP}{dt} = \frac{dR}{dt} - 10(0.8)^{2t+3}$$
,

where t $(t \ge 0)$ is the number of months elapsed since the shop opens.

- Find the total profit of the shop in the first 12 months since the shop opens. (i)
- Estimate the rate of change of the total profit of the shop after a very long time. (ii)

Answers written in the margins will not be marked

$$\frac{d^{3}R}{dt^{3}} = \frac{(e^{0.5t} + 2.5e^{-0.5t})(2e^{0.5t} + 5e^{-0.5t} - 5) - (e^{0.5t} - 2.5e^{-0.5t})(2e^{0.5t} - 5e^{-0.5t})}{(2e^{0.5t} + 5e^{-0.5t} - 5)^{2}}$$

$$= \frac{-5\ell^{0.5t} - 1.25\ell^{-0.5t} + 20}{(2\ell^{0.5t} + 5\ell^{-0.5t} - 5)^{\nu}}$$

$$= \frac{-5(4\ell^{t} + 16\ell^{0.5t} + 5\ell^{-0.5t} - 5)^{\nu}}{4\ell^{0.5t} (2\ell^{0.5t} + 5\ell^{-0.5t} - 5)^{\nu}}$$

$$e = \frac{(u + \frac{2.5}{u})(2u + \frac{5}{u} - 5) - (u - \frac{2.5}{u})(2u - \frac{5}{u})}{(2u - \frac{5}{u})}$$

$$= \frac{-5u - \frac{12.5}{u} + 20}{(2u + \frac{5}{u} - 5)^{\circ}} = \frac{-5e^{0.5+} - \frac{1.25}{\varrho^{0.5+}} + 20}{(2e^{0.5+} + \frac{5}{\varrho^{0.5+}} - 5)^{\circ}}$$
$$-5u - \frac{12.5}{u} + 20 = 0$$

$$-5u-12.5+20=0$$

$$-e^{\circ.6t} = 0.775255128$$
 $-e^{\circ.5t} = 3.224744871$

Answers written in the margins will not be marked

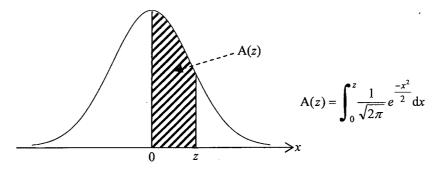
t 105t52.3417 t=2.3417 t71.3417
$\frac{d^2R}{d^2r}$ + 0 - 1
dp df attains its max. value at t= 2.3417
$\frac{2e^{0.5(2.34171}-5e^{-0.5(2.3417)})}{2e^{0.5(2.34171}+5e^{-0.5(2.3417)}-5}$
= 3.6330 thousand dollars
< 9 thousand dollars
No. It doesn't exceed.
bi) $R = \int_{0}^{12} \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} + 5e^{-0.5t} + 5} + 2 dt$ Let $u = 2e^{0.5t} + 5e^{-0.5t} + 5$ $= \int_{12}^{2e^{6} + 5e^{-6} + 5} \frac{2}{u} + 2 du$ Let $u = 2e^{0.5t} + 5e^{-0.5t} + 5$ $\frac{du}{dt} = e^{0.5t} - 2.5e^{-0.5t}$
= [2/n(u) + 2u] 2e6+5e-6+5
= 21n(2e6+5e6+5)+4e6+10e6+100-21n12-29
10 (12 (0, 8) 2++> dt
$= 10 \cdot \left[\frac{(0.8)^{24+3}}{(n0.8)^{0}} \right]^{12}$ $= 10 \cdot \left[\frac{(0.8)^{24+3}}{(n0.8)^{0}} - \frac{0.8^{3}}{(n0.8)^{0}} \right]$
[no.8 - [no.8)
Total profit = 1577.8589 thousand dollars.

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Standard Normal Distribution Table

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z ($z \ge 0$). Areas for negative values of z can be obtained by symmetry.



Level 4 Exemplar 2
2024-DSE MATH EP M1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY

HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2024

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Candidate Number									

MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8:30 am – 11:00 am (2½ hours) This paper must be answered in English

INSTRUCTIONS

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of TWO sections, A and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown.
- (6) Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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SECTION A (50 marks)

The table below shows the probability distribution of a discrete random variable X, where a and b are constants such that (6 < b < 15).

				ð	
x	0	3	6	b	15
P(X=x)	0.3	а	0.1	0.2	0.2

It is given that Var(5X) = 739.

- Find a and b. (a)
- (b) Let C be the event that $0 < X \le 7$.
 - Let D be the event that $4 < X \le 15$. Are C and D independent? Explain your answer.

Let E be an event such that $P(E) \neq 0$. If C and E are mutually exclusive, write down the greatest possible value of P(E).

(7 marks)

Answers written in the margins will not be marked

$$Var(x) = E(x^{2}) - [E(x)]^{2}$$

$$= [(0)^{2}(0.3) + 3^{2}(0.7) + 6^{2}(0.1) + b^{2}(0.7) + 15^{2}(0.7)]$$

$$- [0x0.3 + 3(0.7) + 6(0.1) + 0.7b + 15(0.7)]^{2}$$

$$= (50.4 + 0.2b^{2}) - (4.2 + 0.7b)^{2}$$

$$4b^2-4xb+80=0$$
 $b=8$ or $\frac{5}{5}$ (ref)

by Proj= 0.240.1=0.3	
P(D)=0.1+0.2+0.2=0.5	
P(CID) = P(4 < X < 7)	
0.5	
$= \frac{0.1}{0.5}$	
= 0.7	
": Pce> # pccID>	
C and D are not independent.	
bii) p(cne)=0	
P(c)+ ME) - P(CUE) = 0	·
PLE)-PLOUE) =-0.3	
Pies-(1-pic/ne/)')=-0.3	
PUD 's greatese possine value is 0.3.	

- 2. In an orchestra, $\frac{3}{5}$ of the members wear glasses. Among the male members, $\frac{4}{9}$ of them wear glasses. The probability that a randomly selected member is a female not wearing glasses is $\frac{3}{20}$.
 - (a) Given that a randomly selected member does not wear glasses, find the probability that the member is a female.
 - (b) Find the probability that a randomly selected member is a female wearing glasses.

(6 marks)

Answers written in the margins will not be marked.

a) Let p be the probability of a man in an orchesera.

(4)p+((1-3/2C1-p)	= -3	<u>}</u>
4p+ -	7-47 10-47	= -	3

 $-\frac{73}{180}p = -\frac{1}{4}$

Required probability: $(1-\frac{45}{73})(\frac{3}{20})$

= 146 =0.143 f38 616... = 0.1438 (con to 4 d.p.)

b) Required probability: $(1-\frac{45}{73})(\frac{17}{20})$ = $\frac{119}{365} = 0.326027397... = 0.3260$ (cor. to 4d.y.)

3.	When a coin is tossed, the probability of getting a tail is p , where $0 . When the coin is tossed 20 times, the ratio of the probability of getting 1 tail to the probability of getting 3 tails is 49:57.$
	(a) Find p .
	(b) The coin is tossed k times. Find the least value of k so that the probability of getting at least 1 tail is greater than 0.85.
	a) $C_{i}^{30}(p)(1-p)^{i9}$ 49
	$C_3^{20}(p)^3(r-p)^{17} = 57$
	1140 p (1-12)19 = 55860 p3 (1-p)17
	$\frac{(-\gamma p + p^2)^2}{(-\gamma p + p^2)^2} = 49p^2$
	1-7p+pr = 49p2
	$-4fp^2-2p+1=0$
	48p2+xp-1 = 0
	p = 0.125 or -tired)
	p=0.125
	b> 1- C*(0.125)°(1-0.125)* >0.85
	(1-0.125) = 0.15
	kln 0,875 < ln 0,15
	k > 14,20729573
	k > 14.2073 (cor.to 4dip.)
	i The lease value of k 15 15.

4.	The weekly revision time of each student in a school follows a normal distribution with a mean of μ hours. A random sample of 81 students is drawn from the school. The mean and the standard deviation of the weekly revision time of these students are 13 hours and 1.75 hours respectively.
	(a) The width of a β % confidence interval for μ is 0.7. Find β .
\$	It is given that there are 36 boys in the sample, and the mean and the standard deviation of the weekly revision time of these boys are 12.5 hours and 2 hours respectively. Find the standard deviation of the weekly revision time of the girls in the sample.
	[Hint: The sample standard deviation is $\sqrt{\frac{1}{n-1}} \left(\sum_{i=1}^{n} x_i^2 - n\overline{x}^2 \right)$.]
	(6 marks) $ \lambda \in C_{197} = 0.7 $
	a) $2 \ge (\frac{1.75}{181}) = 0.7$ $\ge = 1.8$
	B % = 0.4641X2
	β = 0.4641x2 β = 92.82
	B=92.82
	by Required Standard deviation:
	1 745
	N(81-36)-1 =1

- Expand $\frac{2}{a^{nx}}$ in ascending powers of x as far as the term in x^3 .
- Consider the expansion of $(1+4x)^m \oint \frac{2}{e^{nx}}$, where m is a positive integer. The coefficients of x and x^2 in the expansion are 24 and 980 respectively. Find the coefficient of x^3 in the expansion. (7 marks)

 $= 2\left(1-nx+\frac{(-nx)^2}{r!}+\frac{(-nx)^3}{1!}+\cdots\right)$

 $= \frac{2(1-nx+\frac{n^2x^2}{2}-\frac{n^3x^3}{6}+\dots)}{2-2nx+n^2x^2-\frac{n^3}{3}x^3+\dots}$

by $(1+4x)^m + \frac{\nu}{e^{nv}}$

= Co(4x) 0(1) m+ c, (4x) (1) m++ c, (4x) 2(1) m-+ c, (4x) 3(1)

 $= 1 + \frac{4m\chi + \frac{m}{(m)(m-1)}}{2} \frac{(16x^{2})^{4} + 2 - m\chi + n^{2}\chi^{2} - \frac{3}{12}\chi^{2} + \dots}{m(m-1)(m-1)} \frac{64\chi^{3}}{3}$

= $1 + 4mx + (8m^2 - 8m)x^2 + 2 - 2nx + n^2x^2 - \frac{n^3}{3}x^3$

 $\frac{4(3^{2}m^{3}-32m^{2}+\frac{64}{3})\chi^{3}}{=3+(4m-m)\chi+(4m^{2}-4m+n^{2})\chi^{2}}$

 $\frac{4\left(\frac{32}{3}m^{3}-32m^{2}+\frac{64}{3}-\frac{n^{3}}{3}\right)\chi^{3}}{\text{for coeff of }\chi^{2}}$ $\frac{4\left(\frac{32}{3}m^{3}-32m^{2}+\frac{64}{3}-\frac{n^{3}}{3}\right)\chi^{3}}{\text{coeff of }\chi^{2}}$ $\frac{4\left(\frac{32}{3}m^{3}-32m^{2}+\frac{64}{3}-\frac{n^{3}}{3}\right)\chi^{3}}{\text{coeff of }\chi^{2}}$ $\frac{4\left(\frac{32}{3}m^{3}-32m^{2}+\frac{64}{3}-\frac{n^{3}}{3}\right)\chi^{3}}{\text{coeff of }\chi^{2}}$

By solving, m=11, n=10

For coeff of 23: (32)(11)3-32(11)2+64-103

(a)	Let $e^u = (x^2 + x + e)^{2x+1}$.
•	(i) Express u in the form of $p(x)\ln(q(x))$, where $p(x)$ and $q(x)$ are polynomials.
	(ii) Express $\frac{d}{dx}e^u$ in terms of x . Explain
(b)	The equation of the curve Γ is $y = (x^2 + x + e)^{2x+1}$. Denote the point of intersection of Γ and the y-axis by H . Find the equation of the tangent to Γ at H . (7 marks)
aī)	$e^{h} = (x^{2} + x + e)^{2x+1}$
	$= (2x+1) \ln(x+x+e)$
ali)	de 2ln(x+x+e)+(xx+1)*(x+x+e)
67	y=(x+x+e)2x+1
•	y: (x + x+e) 2x+1 on - 2h(x + x+e) + (xx+1) (x+x+e)
	$\frac{dy}{dx} _{\chi=0}=2+\frac{1}{e}$
	For X=0, U= e
487-047	For x=0, y=e Required equation is: y-e = >+ t
***************************************	- X
***************************************	y-e = (7+t)x $y = (2+t)x+e$
	y = (>+t)x+e

,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	

7.	A computer programme adjusts the length and the breadth of a rectangular digital picture, such that the length of its diagonal remains constant while its breadth decreases at the constant rate of 0.5 cm s ⁻¹ . Initially, the	
	length and the breadth of the picture are 20 cm and 15 cm respectively. Denote the breadth of the picture by x cm. Find the rate of change of the area of the picture when $x = 7$. (4 marks)	
i.	Area = length x breadth	
	leng th=/120+157-x	
	$\frac{dA}{dt} = \frac{dA}{dx} \cdot \frac{dx}{dt}$	
	$ \frac{A = (x - x^2)^{\frac{1}{2}}}{Ax} = (x - x^2)^{-\frac{1}{2}} (-x x) $ $ = -x(x - x^2)^{-\frac{1}{2}} (-x x) $	arked.
	MA = +(>5 - x') - (->x)	t be m
	= - ス(レケー オン)-た	Answers written in the margins will not be marked
0	$\frac{dA}{dt} = -\chi(25 - \chi^2)^{-\frac{1}{2}}(-0.5)$	rgins v
•	dA/x=7=1.7930149>9m.	the ma
	=1.7930 cm²/s ceor.to4dp.)	ten in
		s writ
		Answei
		1

(8.)X	Year (a) Using the Standard Normal Distribution Table on page 24, evaluate $\int_0^{0.5} e^{\frac{-x^2}{2}} dx$
	(b) Consider the curve $C: y = (2x-1)e^{\frac{-x^2}{2}}$, where $x \ge 0$. Using the result of (a), find the area of the region bounded by C , the x-axis and the y-axis.
	a) $\int_{0}^{2} \frac{1}{\sqrt{\lambda \tau u}} e^{-\frac{x^{2}}{2}} dx$ (7 marks)
	$= \frac{1}{\sqrt{2\pi}} \int_0^{0.5} e^{-\frac{x^2}{2}} dx$
	= to.19.150
	= 0.076397446m = 0.0764
	b) Regulard onen; (7x-1) e = dx = 2e x [x] = e =
	· · · · · · · · · · · · · · · · · · ·
	= 0.057298085 = 0.0573 Sq mits
i	

4	 ***************************************
•	·

SECTION B (50 marks)

- The weight of each pumpkin in a large market follows (normal distribution with a mean of μ kg and a 9. standard deviation of σ kg. It is given that 30.85% of the pumpkins in the market each weighs more than 5.7 kg while 78.88% of the pumpkins each weighs between $(\mu-1.5)$ kg and $(\mu+1.5)$ kg.
 - Find μ and σ . (a)

(3 marks)

- Suppose that 16 pumpkins are randomly chosen in the market. Find the probability that the (b) mean weight of these pumpkins does not exceed 5.4 kg. (2 marks)
- (c) The following table shows the grades and the prices of the pumpkins in the market.

Weight of a pumpkin (W kg)	<i>W</i> ≤ 3.6	$3.6 < W \le 5.7$	W > 5.7
Grade	С	В	Α
Price (\$)	50	80	100

Suppose that 8 pumpkins are randomly chosen in the market and these pumpkins are put into a trolley.

- Find the expected price of the pumpkins in the trolley. χ δ ? (i)
- Find the probability that there are at least 5 grade B pumpkins and at least 1 grade A pumpkin (ii) in the trolley.

Answers written in the margins will not be marked

$$P(8) > 5.7 = 0.3085$$

 $P(8) = 5.7 - 11$

-	
	012 PCW 83.67 = PLZE 3.6-5.1
	= 0.5-0.3144
	= 0.1056
	PC3.6 <wss.7>= PC3.6-5.1<= \(\frac{5.7-5.1}{1.2}\)</wss.7>
B	= 0.3944+0.1915
	= 0.5859
1	Prw>5.7>= 1-0.1056-0.58xg
A	= 0.3085
	Experted price of the pumptins in the trolley =
	\$ [50(0,105b)+ fo(0,5859)+100(0,30fs)]
rked.	= \$ 83.0127
be ma	cii) Required probability:
swers written in the margins will not be marked	C. (0.5859) 5 (0.3085) C, (0.0056) + C 5 (0.5859) 6 (0.3015)
ins wi	(0,1046) (1,
marg	+ C5 (0.5859) (0.3080) + C6 (0.5859) 6(0.3045)(0.1006)C,
in the	+ C6 (0.5819) (0.3085) + C3 (0.5859) 7 (0.3085)
ritten	= 0,338280334
vers w	= 0.3383 (Cor. to 4d.p)
Answ	

0.	A coi	urier delivers goods every day. The number of delays in delivery on a day follows a Poisson distrib	
•		a mean of 1.6. A day is regarded as smooth if there are fewer than 3 delays on that day.	diion
	(a)	Find the probability that a certain day is <i>smooth</i> . $\mathcal{K} \in \mathcal{F}$ (2 m	arks)
	(b)	Find the probability that all the 7 days in a certain week are <i>smooth</i> . (2 m	arks)
	(c)	Given that all the 7 days in a certain week are <i>smooth</i> , find the probability that ther exactly 10 delays in that week. (4 m	e are arks)
	(d)	Given that there are no delays in at least 2 days in a certain week, find the probability all the 7 days in that week are <i>smooth</i> . (4 m	/ that arks)
	ad	Required probability:	
		e-1.6 (1.6° + 1.6' + 1.6°)	
	_	0.783388489	
	=	0.7834 Ceor. to 4d.p.J	
	62	Regulared probability.	
		Cv. 7834)7	
	5	= 0.181018883	
	2	= 0. (to (conto fd.p.)	
	<u> </u>	Probability of howing 2 delays a day. e-1.61.6	
	Re	probability: (0.1818/83) C7 (e-1.61.62) (e-1.61.62))2
	,	0.16018883	
		= 0,0009866671-1	
	***************************************	= 0.0010 (cor-to 4d.p.)	
l	27 R	equired probability. 81018883-[C7(e-1.61.60)(e-1.61.61+e-1.61.62)+C7(e-1.61.61+e-1.61.61)	
		[1-C](e-1.61.6°)°(1-e-1.61.6°)7	
	441111111111111111111111111111111111111	$-c^{7}\left(\frac{e^{-1.6(1.6')}}{(1-e^{-1.6(1.6')})}\right)^{6}$	
	> 0	1,2425}6315	
	= 0	. 2475 (corto 4d.p.)	
	***************************************	·	

		ALUMANIA EMININI MANAMANIA MANAMANIA MANAMANIA MANAMANIA MANAMANIA MANAMANIA MANAMANIA MANAMANIA MANAMANIA MAN		
mantaga di Balkata di Balkata da Afrika		***************************************		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
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		WILLIAM TO THE TOTAL OF THE TOT	 	
11.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1				
AMANUTURA STATEMENT OF THE PROPERTY OF THE PRO				
	,			

$$P = a(-t^2 + 10t + 8)e^{bt}$$
,

where a and b are constants, and t $(0 \le t \le 4)$ is the number of hours elapsed since 7 am on that day. It is found that $\ln\left(\frac{P}{-t^2 + 10t + 8}\right)$ is a linear function of t, and the graph of this linear function passes through the point (3, -0.1) and the intercept on the horizontal axis is 2.5.

- (a) Express $\ln\left(\frac{P}{-t^2 + 10t + 8}\right)$ as a linear function of t. (1 mark)
- (b) Find the exact values of a and b. (3 marks)
- (c) Using the trapezoidal rule with 4 sub-intervals, estimate the accumulative rainfall of city M from 7 am to 11 am on that day. (2 marks)
- (d) The accumulative rainfall of city N on the same day increases at a rate of Q mm per hour. It is given that

$$Q = \frac{16(2t+5)e^{0.4t}}{4te^{0.4t}+3} ,$$

where t ($0 \le t \le 4$) is the number of hours elapsed since 7 am on that day.

- (i) Find $\int Q dt$.
- (ii) Someone claims that the sum of the accumulative rainfalls of city M and city N from 7 am to 11 am on that day is greater than 160 mm. Do you agree? Explain your answer.

(8 marks)

$$\frac{P = a(-t^2 + 10t+8)e^{bt}}{\frac{P}{-t^2 + 10t+8}} = ae^{bt}$$

o) P=e 015 (-t2+10+18)e
$\int_0^4 P dt = \frac{4-0}{4} \left[f(0) + f(1) + f(1) + f(1) + f(1) \right]$
= 34.63957475
= 34.6395 mm (cor. to 4dp)
di) folt) at
$\frac{du}{dt} = 4e^{0.4t} + 9t(0.4)e^{0.4t}$
$= e^{6.4\xi}(4+1.6t)$ $dt = \frac{du}{e^{0.4\xi}(4+1.6t)}$
of to 16(>+15)e 0.4+ du = 0.4+(411.6+)
were written in the markins will not be marked as $\frac{16(3)(4+5)}{2} = \frac{16(3)(4+5)}{2} =$
= no ∫ tr du
= 20 lululte
$= 20 \ln 4te^{0.4t}+3 +C$
din city N rainfall from Jam to llam.
[20ln[4te"43]]
= 66.22266184
= 66.22) Ja Carrelo Edip.)
For cuy M, P=e-0150-t>Holt8)e
$\frac{df}{dt} = e^{-0.24}(-0.2)(e^{-0.3})(-t^2+10+1)$
+(->t+10)e-012+e-013
$= (e^{-0.2t})(e^{-0.5})[-0.2(-t^2+10t+8)-2t+10]$
= (e (0.2t ->t-1.6->+1.6)
= (e-+)(e-0.5.)(0.242-46.4)



Let R be the total revenue (in thousand dollars) of an online shop. It is given that

$$\frac{dR}{dt} = \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} + 5e^{-0.5t} - 5} + 2,$$

where $t \ (t \ge 0)$ is the number of months elapsed since the shop opens.

- (a) Does the greatest rate of change of the total revenue of the shop exceed 4 thousand dollars per month? Explain your answer. (4 marks)
- (b) Let P be the total profit (in thousand dollars) of the shop. It is given that

$$\frac{dP}{dt} = \frac{dR}{dt} - 10(0.8)^{2t+3}$$
,

where t ($t \ge 0$) is the number of months elapsed since the shop opens.

- (i) Find the total profit of the shop in the first 12 months since the shop opens.
- (ii) Estimate the rate of change of the total profit of the shop after a very long time.

a) $\frac{dl^2}{dt} = \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} + 5e^{-0.5t}} + 2$ (9 marks)

Answers written in the margins will not be marked

dip (reoute	5e-0.81 (2e0-81 (08) -5	(-05)e-015t)
- (>1 ×5	Je = 5 = + 5 (-0.5) e - 0.50) (76°56-56-0.58)
	(20086 to noi.	t 12

•	(20	, ,	
0.66	(e-pose) (.	oxt t	cost,
(2e +	5e ->)(. 5e ->(.	e fit	
> - (00,54	50-015t)(>	00.56	0-0.54)
			<u> </u>
0	81 o.5t	->2	
(),e,	450)	

<u></u>	$= \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} - 5e^{-0.5t}} + 2 - 1660.85 + 18$ $= \int_{0}^{12} \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} + 5e^{-0.5t}} + 2 - 1060.85 + 183 dt$
	e ost45e-ost-5
000	20.5)e 0.5t + 51-0-5)e 0.5t
	e 0.5t-5e-0.5t
for tz	
D- 2 [l	$[12, u^{2}] = 2e^{4} + 5e^{-5}$ $[12, u^{2}] = 2e^{4} + 5e^{-6} + [2t]_{2}^{2} - [0] = [0.8 \times 10]_{2}^{2}$ $[12, u^{2}] = 2e^{4} + 5e^{-6} + [2t]_{2}^{2} - [0] = [0.8 \times 10]_{2}^{2}$ $[12, u^{2}] = 2e^{4} + 5e^{-6} $
= 32,	5x79x02
= 32,3	522f thousand dollars.
lim of	2e 0.5t-5e-0.5t +2 -10 (0 B) 2++3
$= \frac{2-6}{2+6-5}$	ナレーロ
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Standard Normal Distribution Table

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z ($z \ge 0$). Areas for negative values of z can be obtained by symmetry.

