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Level 3 Exemplar 1
2024-DSE MATH EP M1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY

HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2024

Please stick the barcode label here. Candidate Number

MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8:30 am – 11:00 am (2½ hours) This paper must be answered in English

INSTRUCTIONS

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of TWO sections, A and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown.
- (6) Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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SECTION A (50 marks)

1. The table below shows the probability distribution of a discrete random variable X, where a and b are constants such that 6 < b < 15.

			K		
x	0	3	6	b	15
P(X=x)	0.3	а	0.1	0.2	0.2
		1			

It is given that Var(5X) = 739.

- (a) Find a and b.
- (b) Let C be the event that $0 \le X \le 7$.
 - (i) Let D be the event that $4 < X \le 15$. Are C and D independent? Explain your answer.
 - (ii) Let E be an event such that $P(E) \neq 0$. If C and E are mutually exclusive, write down the greatest possible value of P(E).

(7 marks)

Answers written in the margins will not be marked.

(b) (i)
$$P(O < x \in I) = P(x = 3) + P(x = 6) = 0.3$$

 $P(U < x \in I) = P(X = 6) + P(X = 8) + P(X = 15)$
 $= 0.5$

For P(CND) = P(X=6)=0.1

i not independent

(17) 0.7

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- 2. In an orchestra, $\frac{3}{5}$ of the members wear glasses. Among the male members, $\frac{4}{9}$ of them wear glasses. The probability that a randomly selected member is a female not wearing glasses is $\frac{3}{20}$.
 - (a) Given that a randomly selected member does not wear glasses, find the probability that the member is a female.
 - (b) Find the probability that a randomly selected member is a female wearing glasses.

(6 marks)

Answers written in the margins will not be marked.

(a) P(female | not wear) = P(female 1 not wear)

is required prob = $(1-p)(\frac{1}{20})$ 0.4

= 146

(6) P(female 1 wear) = (1-p)(1/2) = 1/365

3.

- tossed 20 times, the ratio of the probability of getting 1 tail to the probability of getting 3 tails is 49:57.

 (a) Find p.
 - (b) The coin is tossed k times. Find the least value of k so that the probability of getting at least 1 tail is greater than 0.85.

When a coin is tossed, the probability of getting a tail is p, where 0 . When the coin is

(6 marks) $\frac{(a) P(fail) = P}{(P) (P) (P)^{(q)}} = 49$

 $\frac{C_{17}^{\infty}(p^{3})(1-p)^{17}}{(1-p)^{19}} = \pm 1860 p^{3} (1-p)^{17}$ $\frac{(1-p)^{19}}{(1-p)^{17}} = \pm 1860 p^{3}$

1 - 2p + p2 = (9p2 p= -6 (-ve rej) or 0.125

(b) 1-P(0 fail) = 0.85 $1-(1-P)^{k} = 0.85$

(1-p)k = 0.15

k=14,2073 (4d

i least value of k is is

- 4. The weekly revision time of each student in a school follows a normal distribution with a mean of μ hours. A random sample of 81 students is drawn from the school. The mean and the standard deviation of the weekly revision time of these students are 13 hours and 1.75 hours respectively.
 - (a) The width of a β % confidence interval for μ is 0.7. Find β .
 - (b) It is given that there are 36 boys in the sample, and the mean and the standard deviation of the weekly revision time of these boys are 12.5 hours and 2 hours respectively. Find the standard deviation of the weekly revision time of the girls in the sample.

[Hint: The sample standard deviation is $\sqrt{\frac{1}{n-1} \left(\sum_{i=1}^{n} x_i^2 - n\overline{x}^2 \right)}$.

(6 marks)

Answers written in the margins will not be marked.

(a) 2 (d p4) (1.75) = 0.7

B = 92.82

(b) number of girl in sample is 45 For boy4, sample SD = 1 (36 xi - 56x)

2= 1 (16 x 2 - 165)

(xi2 - 16x)

For girls, semple sD = 1 (= x(2 - 45 x 2)

36 (1215) + sample mean of girls (45) = 13

Sample mean of girl i, required SD = 1 (us xi2 - 8080.2)

5.	Let i	n be a	positive	number.
----	-------	--------	----------	---------

- (a) Expand $\frac{2}{e^{nx}}$ in ascending powers of x as far as the term in x^3 .
- (b) Consider the expansion of $(1+4x)^m + \frac{2}{e^{3x}}$, where m is a positive integer. The coefficients of x and x^2 in the expansion are 24 and 980 respectively. Find the coefficient of x^3 in the expansion.

 (7 marks)

 $\frac{(a)_{1}e^{-hx}}{(a)_{1}e^{-hx}} = 2\left(1 + \frac{-hx}{1!} + \frac{(-hx)^{2}}{2!} + \frac{(-hx)^{3}}{3!} + \cdots\right)$ $= 2 - 2hx + h^{2}x^{2} - \frac{1}{2}h^{3}x^{3} + \cdots$

(b) $[1+4x]^{M} = 1^{M} + C^{M} (1)^{M-1} (4x)^{1} + C^{M} (1)^{M-2} (4x)^{2} + C^{M} (1)^{M-2} (4x)^{2}$

 $= (+ 4mx + \frac{(m-1)m}{2} + \frac{(m-1)(m-2)}{6} + \frac{32}{2} + \frac{32}{2}$

 $\frac{(1+4x)^{2}+\frac{1}{6x^{2}}}{(1+4x)^{2}+\frac{1}{6x^{2}}}=\frac{(1-2x)^{2}+x^{2}-\frac{1}{3}x^{3}+x^{3}+x^{2}-\frac{1}{3}(1+4x)^{2}}{(1+4x)^{2}+\frac{1}{6x^{2}}}$

= 3+(4m-2n)x+[8m(m-1)+n+]x+

 $\frac{1}{3} m (m-1)(m-2) - \frac{1}{3} m^{3} x^{5} + \dots$ $\frac{1}{3} m (m-1)(m-2) - \frac{1}{3} m^{3} x^{5} + \dots$

By comparing coeff, 4m-2n=24, 2m-12=n

8m²-8m+2y-48m+12-980=0

m = 11 or - 3 (rej)

n= 2(11) -n=10

1 coeff of x3 = 32 (11) (10)(9) - 1 103

= 40680

6.	(a)	Let	$e^{u} = (x^{2} + x + e)^{2x+1}$
----	-----	-----	----------------------------------

- Express u in the form of $p(x)\ln(q(x))$, where p(x) and q(x) are polynomials. (i)
- Express $\frac{d}{dx}e^u$ in terms of x. (ii)
- The equation of the curve Γ is $y = (x^2 + x + e)^{2x+1}$. Denote the point of intersection of Γ and (b) the y-axis by H. Find the equation of the tangent to Γ at H.

(7 marks)

y = 2 ln (x2+x+e)+

Answers written in the margins will not be marked

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Ay	ea = 20, U = 300 cm² (t=0)
. <u>A</u>	$rea = vo \times cm^2 \qquad (t>0)$
di	A dA dx
9	t dx dt
1	5-7 / t= 16
•	1
· /	
 wh	in x=15. A=30
	= x= (41), A = 280
` ` `	when X decrease 1 A decrease to
	, A
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	at tak tox (10x). (()
	= 140,

8.	(a) Using the Standard Normal Distribution Table on page 24, evaluate $\int_0^{0.5} e^{\frac{-x^2}{2}} dx$.	
	(b) Consider the curve $C: y = (2x-1)e^{\frac{-x^2}{2}}$, where $x \ge 0$. Using the result of (a), find the area of the region bounded by C , the x -axis and the y -axis. (a) $A(0.5) = \int_0^{0.5} \int_0^{-x^2} dx$ (7 marks) $A(0.5) = \int_0^{0.5} \int_0^{-x^2} dx$ $A(0.5) = \int_0^{0.5} \int_0^{-x^2} dx$	
	(6) $M=0$ $2x-(20)$ or $e^{-\frac{1}{2}}=0$ (rej) $x = \frac{1}{2}$ required one = $\int_{0.5}^{0.5} (2x-1) e^{-\frac{1}{2}} dx$ = $\int_{0.5}^{0.5} 2x e^{-\frac{1}{2}} dx - \int_{0.4}^{0.4} e^{-\frac{1}{2}} dx$ = $\int_{0.5}^{0.5} 2x e^{-\frac{1}{2}} dx - 0.46001 = 0.24$	Answers written in the margins will not be marked.

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SECTION B (50 marks)

- 9. The weight of each pumpkin in a large market follows a normal distribution with a mean of μ kg and a standard deviation of σ kg. It is given that 30.85% of the pumpkins in the market each weighs more than 5.7 kg while 78.88% of the pumpkins each weighs between $(\mu 1.5)$ kg and $(\mu + 1.5)$ kg.
 - (a) Find μ and σ .

(3 marks)

- (b) Suppose that 16 pumpkins are randomly chosen in the market. Find the probability that the mean weight of these pumpkins does not exceed 5.4 kg. (2 marks)
- (c) The following table shows the grades and the prices of the pumpkins in the market.

Weight of a pumpkin (W kg)	<i>W</i> ≤ 3.6	$3.6 < W \le 5.7$	W > 5.7
Grade	С	В	Α
Price (\$)	50	80	100

Suppose that 8 pumpkins are randomly chosen in the market and these pumpkins are put into a trolley.

- (i) Find the expected price of the pumpkins in the trolley.
- (ii) Find the probability that there are at least 5 grade B pumpkins and at least 1 grade A pumpkin in the trolley.

(6 marks)

Answers written in the margins will not be marked

(b) $P(x < 5.4) = P(t < \frac{5.4-5.1}{100}) = P(t < 1) = 0.3413 + 0.5=0.8413$ i veguired prop = 0.8413 6 116

(c) (i) $P(W \le 3.6) = P(Z \le \frac{3.6 - 5.1}{18}) = P(Z \le -7.25)$

P(W751) = (-0.0002-0.9205=0.079)

***************************************	= \$1, \$\langle \tag{8}
(7	11) P(>5B N > (A) = P(>C, 13, 1A) + P(1C, 513)A + P(0C, 513, 3A) + P(1C, 613, 1A)
	+ P(OC, 613, 2A) +P(OC7B, (A)
	= C\$ · 0,9 205 (C3) 0,07 932 · 0,0002) +
	C8 0.9205 (C3, 0.0793 0.0002)+
	$\frac{C_{50}^{8}}{2005}$ $\frac{C_{50}^{8}}{2005}$ $\frac{C_{50}^{8}}{2005}$ $\frac{C_{50}^{8}}{2005}$ $\frac{C_{50}^{8}}{2005}$
	C& 0.92056 (c, 0.0793 0,0002) + C& 0.92056 (c, 0.07932) +
***************************************	C7 2. 7257 (C; 0.0773)
	·0. 48149648 2 0.4814
	0. 4016 0.49 ~ 0. 4414

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10.	A courier delivers goods every day. The number of delays in delivery on a day follows a Poisson distribution with a mean of 1.6. A day is regarded as <i>smooth</i> if there are fewer than 3 delays on that day.
	(a) Find the probability that a certain day is smooth. O, I, I (2 marks)
	(b) Find the probability that all the 7 days in a certain week are <i>smooth</i> . (2 marks)
	(c) Given that all the 7 days in a certain week are <i>smooth</i> , find the probability that there are exactly 10 delays in that week. (4 marks)
	(d) Given that there are no delays in at least 2 days in a certain week, find the probability that all the 7 days in that week are <i>smooth</i> . (4 marks)
	(a) $P(x(3) = e^{-1.6}(1+1.6+1.6^{2}/2)$ = 0.783378487 ~ 0.7834
	= 0./83378481 ~ 0.7854
	(b) required prob = C) (0.7834) (0.021.66)
	(b) required prob = C7 (0.7834, (0.21.66) = 0.1810/883
	(c) P (10 delays in week all day smooth)
	For exact is delays in week
	regard prob = (3 (P(x=2)) (P(x+2))
	P(x73) = 1 - P(x53)
	= 1-e-(16(1+1,6+1.62+1.63)
	= 0.078.813489
	P(x+v)=P(x=0)+P(x=1)+P(x>3)
	- 0 (1) + 0 (16) + P(X>3) = 0,603744434
	required prob = $C_3(V(x=x)^3)(P(x=0,1)^4)$
	= 0,04586624
	: P(10 delays in week) all day smooth)
	= 0.04586624 = 0.2537821
	0.(8(0) 8883

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$$P = a(-t^2 + 10t + 8)e^{bt},$$

11.

Answers written in the margins will not be marked

where a and b are constants, and t $(0 \le t \le 4)$ is the number of hours elapsed since 7 am on that day. It is found that $\ln\left(\frac{P}{-t^2+10t+8}\right)$ is a linear function of t, and the graph of this linear function passes through the point (3, -0.1) and the intercept on the horizontal axis is 2.5.

The accumulative rainfall of city M on a certain day increases at a rate of P mm per hour. It is given that

(a) Express
$$\ln\left(\frac{P}{-t^2+10t+8}\right)$$
 as a linear function of t . (1 mark)

Find the exact values of a and b. (b)

(3 marks)

- Using the trapezoidal rule with 4 sub-intervals, estimate the accumulative rainfall of city M from 7 am to 11 am on that day.

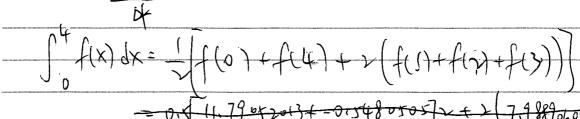
 (2 marks) (c)
- The accumulative rainfall of city N on the same day increases at a rate of Q mm per hour. It is given (d)

$$Q = \frac{16(2t+5)e^{0.4t}}{4te^{0.4t}+3} \ ,$$

where t ($0 \le t \le 4$) is the number of hours elapsed since 7 am on that day.

- Find $\int Q dt$. (i)
- (ii) Someone claims that the sum of the accumulative rainfalls of city M and city N from 7 am to 11 am on that day is greater than 160 mm. Do you agree? Explain your answer.

(8 marks)



+4,633040482 (1.785041281)} = 12 22 822250
= 015[13,1897701]+23,70618306+2(22.94759873
+ 26,524 10203+26,40285(2)]
= 194, 1599 635
(d)(i) [adt = [16(2++5)e0.4+
$\frac{(d)(1)}{(de)^{(4)}} = \frac{(b(2t+5)e^{-4t})e^{-4t}}{(de)^{(4)}} = \frac{(d)(1)}{(de)^{(4)}}$
Let u be $(2t+t)e^{0.4t} \rightarrow \frac{1}{2}$ $du = (20.4t + (2t+5)e^{0.4t}(0.4))dt$
- (2e + 00Te = 1e / 8)
16 (2+++)e = 16 N d+
J 4+e0.4+3 1 1+0.2+
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$$\frac{\mathrm{d}R}{\mathrm{d}t} = \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} + 5e^{-0.5t} - 5} + 2 ,$$

where t ($t \ge 0$) is the number of months elapsed since the shop opens.

- (a) Does the greatest rate of change of the total revenue of the shop exceed 4 thousand dollars per month? Explain your answer. (4 marks)
- (b) Let P be the total profit (in thousand dollars) of the shop. It is given that

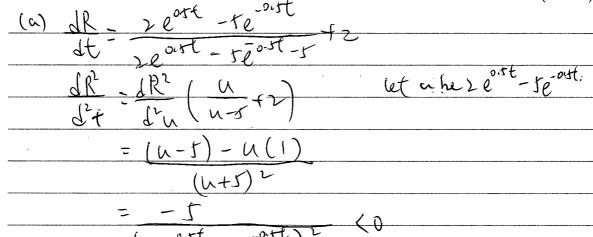
$$\frac{dP}{dt} = \frac{dR}{dt} - 10(0.8)^{2t+3} ,$$

where t $(t \ge 0)$ is the number of months elapsed since the shop opens.

- (i) Find the total profit of the shop in the first 12 months since the shop opens.
- (ii) Estimate the rate of change of the total profit of the shop after a very long time.

(9 marks)

Answers written in the margins will not be marked



For dR =0 0-2eost-5e-ost +2(2eost-5e-ost)

0-2eost-5e-ost + 4eost-10e-ost-10

0 = 6e° 5t - (5e° 5t)

i too is max of rate of change

is not exceed 4 thousand

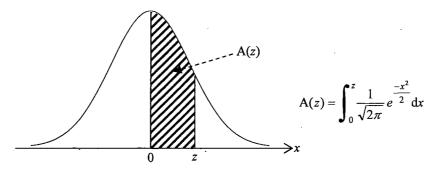
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(55)) (in +700	df dt	= >	-10(() =	- f		
				-				

Standard Normal Distribution Table

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z ($z \ge 0$). Areas for negative values of z can be obtained by symmetry.



Level 3 Exemplar 2
2024-DSE MATH EP M1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY

HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2024

Please stick the barcode label here.										
	Candidate Number									

MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8:30 am - 11:00 am (2½ hours)
This paper must be answered in English

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- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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SECTION A (50 marks)

1. The table below shows the probability distribution of a discrete random variable X, where a and b are constants such that 6 < b < 15.

x	0	3	6	ь	15
P(X=x)	0.3	а	0.1	0.2	0.2

It is given that Var(5X) = 739.

- (a) Find a and b.
- (b) Let C be the event that $0 < X \le 7$.
 - (i) Let D be the event that $4 < X \le 15$. Are C and D independent? Explain your answer.
 - (ii) Let E be an event such that $P(E) \neq 0$. If C and E are mutually exclusive, write down the greatest possible value of P(E).

(7 marks)

Answers written in the margins will not be marked.

$$A) A = (-0.1 - 0.3 - 0.2 - 0.)$$

$$= 0.2_{i}$$

$$E(X_{j}) = \rho_{J}(0.7) + \beta_{J}(0.7) + \beta_{J}(0.7) + \beta_{J}(0.7) + \beta_{J}(0.7)$$

$$= (4.7 + 0.77)$$

$$= 50.4 + 0.16^2 - (4.240.26)^2$$

Fil P(c) = 0.24 0-1	
= 0-3	
P(D) = 0-1 +0,240,2	
P(C \ D) =1	
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(Le gratest value II	
The gratust value of 6771 P(E) =0-7	

- 2. In an orchestra, $\frac{3}{5}$ of the members wear glasses. Among the male members, $\frac{4}{9}$ of them wear glasses. The probability that a randomly selected member is a female not wearing glasses is $\frac{3}{20}$.
 - (a) Given that a randomly selected member does not wear glasses, find the probability that the member is a female.
 - (b) Find the probability that a randomly selected member is a female wearing glasses.

(6 marks)

Answers written in the margins will not be marked.

(2	[ct	7	be	the	probability	#	<u> </u>	mall	member	
	4x+	(1-16-	3)=	3 5		1				
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x = 0.45

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	negrinal		`-	0.45(1-4)+3	
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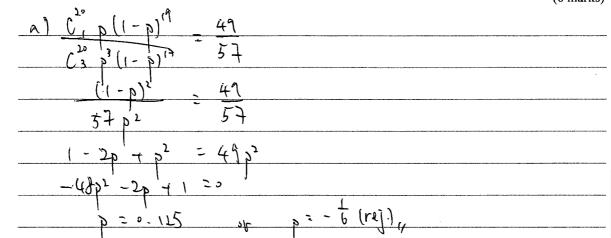
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- Answers written in the margins will not be marked.

- When a coin is tossed, the probability of getting a tail is p, where 0 . When the coin istossed 20 times, the ratio of the probability of getting 1 tail to the probability of getting 3 tails is 49:57.
 - (a) Find p.
 - The coin is tossed k times. Find the least value of k so that the probability of getting at least 1 tail (b) is greater than 0.85.

(6 marks)

Answers written in the margins will not be marked.



b) (.	- co {(-p)k > 9.85	
	(1-p)K <0.15	
	0.875k < 0.15	

Kh 0.875 < h 0-13

/c = 13/+

- 4. The weekly revision time of each student in a school follows a normal distribution with a mean of μ hours. A random sample of 81 students is drawn from the school. The mean and the standard deviation of the weekly revision time of these students are 13 hours and 1.75 hours respectively.
 - (a) The width of a β % confidence interval for μ is 0.7. Find β .
 - (b) It is given that there are 36 boys in the sample, and the mean and the standard deviation of the weekly revision time of these boys are 12.5 hours and 2 hours respectively. Find the standard deviation of the weekly revision time of the girls in the sample.

[Hint: The sample standard deviation is $\sqrt{\frac{1}{n-1} \left(\sum_{i=1}^{n} x_i^2 - n\overline{x}^2 \right)}$.]

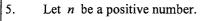
(6 marks)

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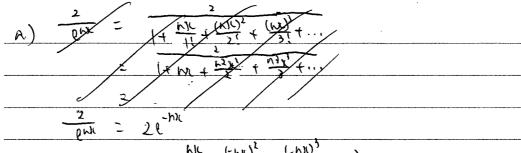
(a) $(3+2\sqrt{37}) - (13-2\sqrt{37}) = 0.7$ $2 = \frac{(.45)}{37} = 0.7$

2 = (-8

: β= 0.4641 (2) (103) = 92.82//



- (a) Expand $\frac{2}{a^{nx}}$ in ascending powers of x as far as the term in x^3 .
- (b) Consider the expansion of $(1+4x)^m + \frac{2}{e^{nx}}$, where m is a positive integer. The coefficients of x and x^2 in the expansion are 24 and 980 respectively. Find the coefficient of x^3 in the expansion. (7 marks)



b)
$$(1+4x)^{m} = 1+c^{m}(1)(4x)+c^{m}(1)(4x)^{2}+c^{m}(1)(4x)^{m}$$

alficing of x in the expansion = 24
$$\frac{M!}{1!(m-1)!} (1)(4) + (-2n) = 24$$

$$4m-2n=24 \longrightarrow n=-i2+2m$$

$$\frac{m!}{2!(m-1)!}(1)(4^2) - \frac{1}{3}n = 965$$

$$\frac{m(m-1)}{2}(1)(4^3) - \frac{1}{3}n = 965$$



6. (a	a) Let	$e^u = (x^2$	$+x+e)^{2x+1}$
-------	--------	--------------	----------------

- (i) Express u in the form of $p(x)\ln(q(x))$, where p(x) and q(x) are polynomials.
- (ii) Express $\frac{d}{dx}e^u$ in terms of x.
- (b) The equation of the curve Γ is $y = (x^2 + x + e)^{2x+1}$. Denote the point of intersection of Γ and the y-axis by H. Find the equation of the tangent to Γ at H.

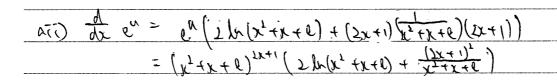
(7 marks)

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$$V = \{x_1 + 1 + 6\}_{3x+1}$$

$$V = \{x_1 + 1 + 6\}_{3x+1}$$

n= (1x+1) lu(x2+x+l),,



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When
$$x=0$$
 $y = (0^2 + 0 + 0)^{2(9)} + 1$

Regular equation is $\frac{g-e}{x} = 2e+1$

T.e (2e+1)x-y+e=0,

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of its diagonal re length and the br	gramme adjusts the length and the breadth of a rectangular digital picture, such that the length amount of the picture are 20 cm and 15 cm respectively. Denote the breadth of the picture are of the picture when $x = 7$. (4 materials)
The	length of diagonal = $\sqrt{15^2 + 20^2}$ = 25 cm
Initio	
	$\frac{-300}{\text{OMEG}} = 3(25^2 - 11^2)$
INC	$A = 625 \times - \times^{3}$
·	$\frac{AA}{Ax} = 625 - 3x^2$
	$\frac{dA}{dx}(x=7 = 625 - 3(7)^{2})$ = 478
	· A
	·
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	8.	(a)	Using the Standard Normal Distribution Table on page 24, evaluate	$\int_0^{0.5} e^{\frac{-x^2}{2}} \mathrm{d}x \ .$
ı			2	

(b) Consider the curve $C: y = (2x-1)e^{\frac{-x^2}{2}}$, where $x \ge 0$. Using the result of (a), find the area of the region bounded by C, the x-axis and the y-axis.

(7 marks)

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SECTION B (50 marks)

- 9. The weight of each pumpkin in a large market follows a normal distribution with a mean of μ kg and a standard deviation of σ kg. It is given that 30.85% of the pumpkins in the market each weighs more than 5.7 kg while 78.88% of the pumpkins each weighs between $(\mu 1.5)$ kg and $(\mu + 1.5)$ kg.
 - (a) Find μ and σ .

(3 marks)

- (b) Suppose that 16 pumpkins are randomly chosen in the market. Find the probability that the mean weight of these pumpkins does not exceed 5.4 kg. (2 marks)
- (c) The following table shows the grades and the prices of the pumpkins in the market.

Weight of a pumpkin (Wkg)	<i>W</i> ≤ 3.6	$3.6 < W \le 5.7$	W > 5.7
Grade	С	В	Α
Price (\$)	50	80	100

Suppose that 8 pumpkins are randomly chosen in the market and these pumpkins are put into a trolley.

- (i) Find the expected price of the pumpkins in the trolley.
- (ii) Find the probability that there are at least 5 grade B pumpkins and at least 1 grade A pumpkin in the trolley.

(6 marks)

Answers written in the margins will not be marked

a)
$$P(2 \times \frac{5.7 - \mu}{5.1 - \mu}) = 0.3085$$

2 31.5

M=5.19

= 0.8413

	urier delivers goods every day. The number of delays in delivery on a day follows a Poisso a mean of 1.6. A day is regarded as <i>smooth</i> if there are fewer than 3 delays on that day. Find the probability that a certain day is <i>smooth</i> .	(2 marks)
(b)	Find the probability that all the 7 days in a certain week are <i>smooth</i> .	(2 marks)
(c)	Given that all the 7 days in a certain week are <i>smooth</i> , find the probability t exactly 10 delays in that week.	hat there are (4 marks)
(d)	Given that there are no delays in at least 2 days in a certain week, find the prall the 7 days in that week are smooth. The required publicity = $\frac{1}{N^{2}} = \frac{e^{-1.6} \cdot 1.6^{N}}{N!}$ ≈ 0.7837549	obability that (4 marks)
<i>_p</i>)	The required probability = (= (1.6.1.0) } 2 0.1810(1883)	
<u> </u>	Let the pubability in (b) be proposed for the proposed of the	
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	Let the probability in (c) be p3	
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1) The inquired probability

- (a) Express $\ln\left(\frac{P}{-t^2 + 10t + 8}\right)$ as a linear function of t. (1 mark)
- (b) Find the exact values of a and b. (3 marks)
- (c) Using the trapezoidal rule with 4 sub-intervals, estimate the accumulative rainfall of city M from 7 am to 11 am on that day. (2 marks)
- (d) The accumulative rainfall of city N on the same day increases at a rate of Q mm per hour. It is given that

$$Q = \frac{16(2t+5)e^{0.4t}}{4te^{0.4t}+3} ,$$

where t ($0 \le t \le 4$) is the number of hours elapsed since 7 am on that day.

(i) Find $\int Q dt$.

Answers written in the margins will not be marked

(ii) Someone claims that the sum of the accumulative rainfalls of city M and city N from 7 am to 11 am on that day is greater than 160 mm. Do you agree? Explain your answer.

(8 marks)

$$\frac{\rho}{(-t^2+10t+b)} = \alpha(-t^2+10t+b)e^{bt}$$

$$\frac{\rho}{(-t^2+10t+b)} = ae^{bt}$$

$$\ln(42+10t+b) = bt + \ln\alpha$$

$$b = \frac{-0.1 - 0}{2.5 - 3}$$

A 11,000,00 A 100,000	2 90.3831 2797 2 90.3838 mm,	
		in construction to the same of
	+ f(t) = e^{-c5}(-t^2 + (ot + b)e^{-2t})	***************************************
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P = e-05 (-t2 +10+ +3) e.2t
= e -0.3+0-24 (-+2)
MP - 0.3+0.24 (-)++12) + (-0.5+2.24 [0.7) (-+2+10++2)
= (-2++10-0.2+ +1.6)
= e (-0.2t +11.6)
$\frac{d^{2}p}{dt} = e^{-0.5 + 0.2t} \left(-0.4t \right) + e^{-0.5 + 0.2t} \left(0.2 \right) \left(-0.2 t^{2} + 11.6 \right)$
20.5 46.24
= e (-0.34.42 -0.34(+2.36)
= e-0.5+0.2+ [-400)[+2 +10+ 1200]
-0.5 to.2t.
= e (-400 (++ 10+ +5 -5) + 23201) = e (-4.0 (++5) + 33201)
20 fin 0 € + 6.44
V
Estimate in (C) is an over-estimated.
Actual accompanies romatell in M < 90.3838
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$$\frac{\mathrm{d}R}{\mathrm{d}t} = \frac{2e^{0.5t} - 5e^{-0.5t}}{2e^{0.5t} + 5e^{-0.5t} - 5} + 2 ,$$

where t ($t \ge 0$) is the number of months elapsed since the shop opens.

- Does the greatest rate of change of the total revenue of the shop exceed 4 thousand dollars per month? Explain your answer. (4 marks)
- Let P be the total profit (in thousand dollars) of the shop. It is given that (b)

$$\frac{dP}{dt} = \frac{dR}{dt} - 10(0.8)^{2t+3} ,$$

where $t \ (t \ge 0)$ is the number of months elapsed since the shop opens.

- (i) Find the total profit of the shop in the first 12 months since the shop opens.
- Estimate the rate of change of the total profit of the shop after a very long time. (ii)

(9 marks)

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r)	Let	w =	20°54 -50°54 -5	
		du =	6°.54 6° 42.56	
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Standard Normal Distribution Table

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944,	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z ($z \ge 0$). Areas for negative values of z can be obtained by symmetry.

